



Course 142A Compilers & Interpreters
Code Analysis

Lecture Week 5
Prof. Dr. Luc Bläser


Last Week - Quiz

```
a = 1;
if (...) {
    a = a + 1;
    b = a;
} else {
    b = 2;
}
c = b + 1;
writeInt(c);
```



How could this be optimized?

Constant Propagation



```
a = 1;
if (...) {
    a = a + 1;
    b = a;
} else {
    b = 2;
}
c = b + 1;
writeInt(c);
```

```
a = 1;
if (...) {
    a = 2;
    b = 2;
} else {
    b = 2;
}
c = 3;
writeInt(c);
```

Copy Propagation



```
...  
c = 3;  
writeInt(c);
```

```
...  
c = 3;  
writeInt(3);
```

Dead Code Elimination

```
a = 1;  
if (...) {  
    a = 2;  
    b = 2;  
} else {  
    b = 2;  
}  
c = 3;  
writeInt(3);
```

writeInt(3);



How to Determine Optimizations?

- Static code analysis = at compile time
 - Statement about all possible runtime cases
- Facilitates optimizations
 - Constant propagation
 - Dead code elimination
 - ...
- But also error detection
 - Reading uninitialized variables
 - Certainly failing runtime checks
 - ...

Today's Topic

- Code Analysis
- Control Flow Graphs
- Dataflow Analysis
- Use Cases

Learning Goals

- Understand dataflow analysis as a generic code analysis method
- Know how to apply it for error detection and optimizations in a compiler

First Analysis Example

```
int a;  
int b;  
int c;  
a = 10;  
if (...) {  
    b = a;  
}  
c = a + b + c;
```



Where do we read uninitialized variables?
How to detect this?

Analyze All Paths

```
int a; int b; int c;
```

a, b, and c uninitialized

```
a = 10
```

b and c uninitialized

```
if (...)
```

b and c uninitialized

b and c uninitialized

```
b = a
```

c uninitialized

a initialized
b possibly uninitialized
c certainly uninitialized

```
c = a + b + c
```

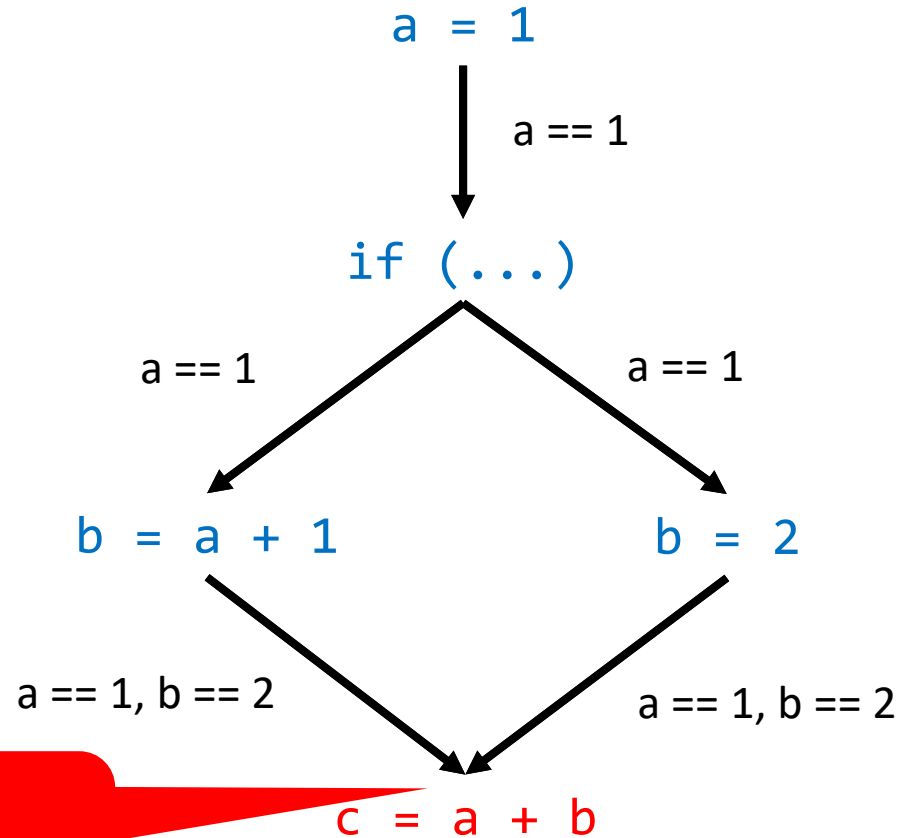
Second Analysis Example

```
a = 1;  
if (...) {  
    b = a + 1;  
} else {  
    b = 2;  
}  
c = a + b;
```



Is the value of c constant?
If yes, what is its value?

Analyze All Paths



a and b are the
same on all paths
 $\Rightarrow c == 3$

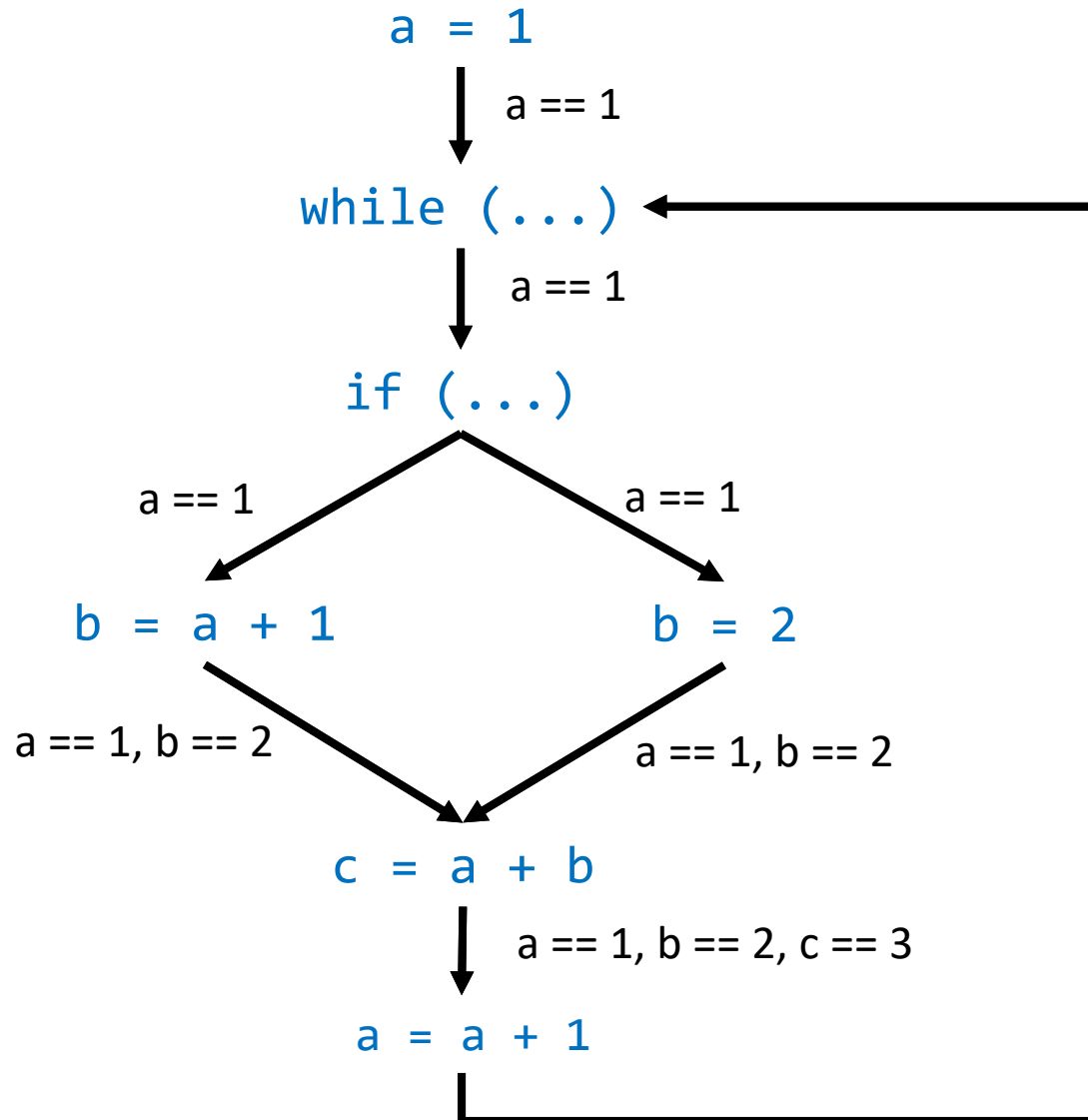
Small Modification

```
a = 1;
while (...) {
  if (...) {
    b = a + 1;
  } else {
    b = 2;
  }
  c = a + b;
  a = a + 1;
}
```

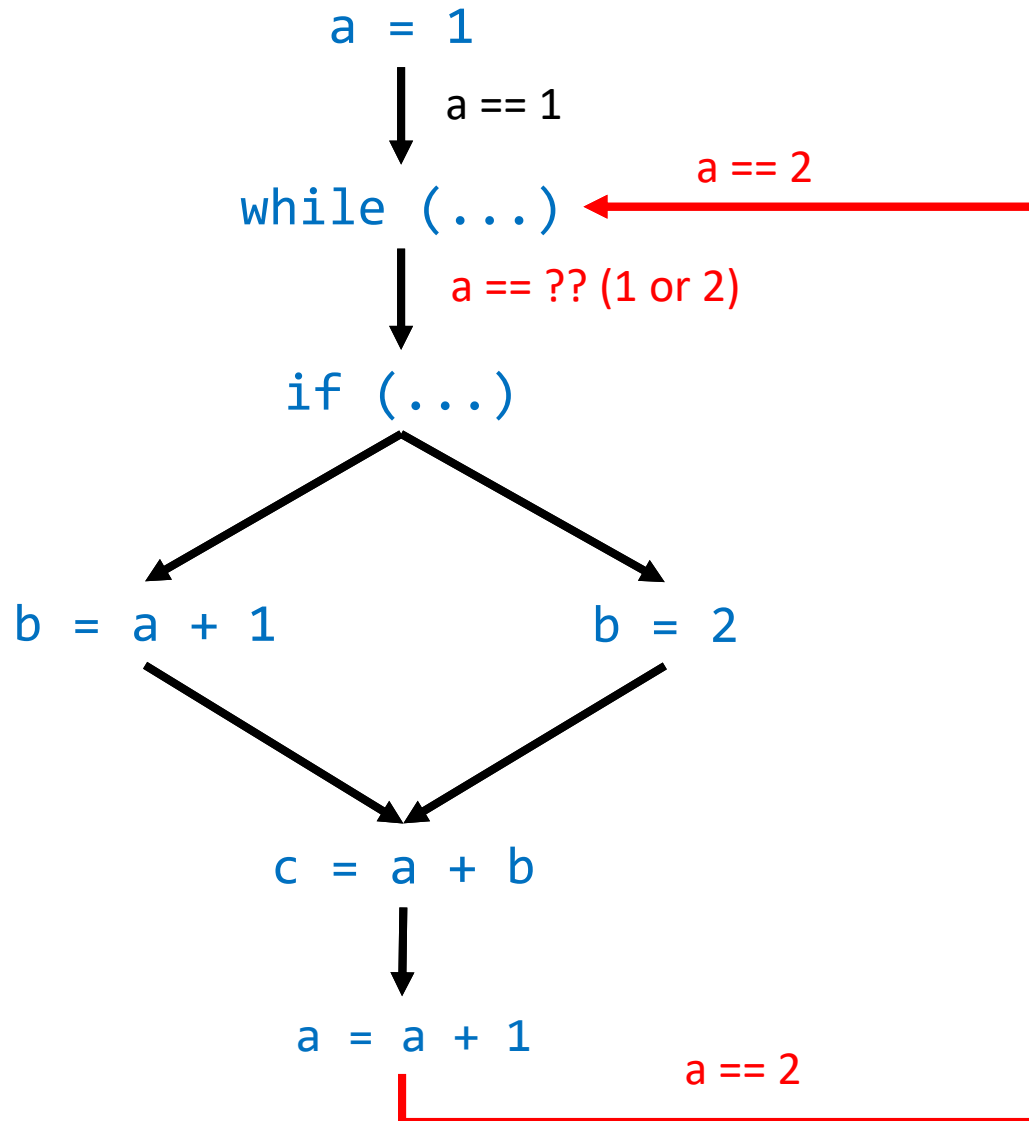


Is c still constant?

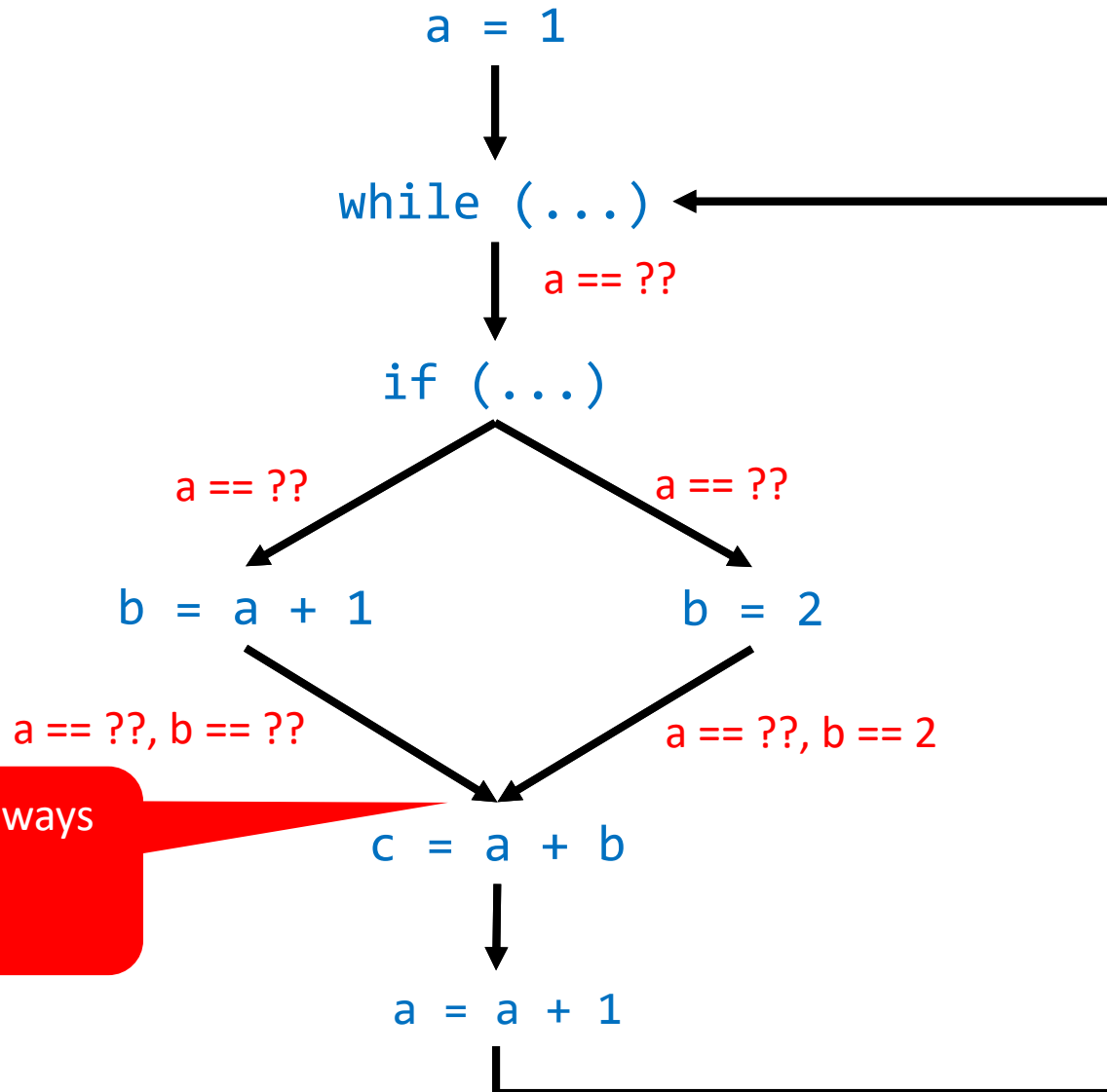
Analyze All Paths



Analyze All Paths



Analyze All Paths



a and b not always constant
=> c neither

Our Approach

- Construct a Control Flow Graph
 - Graph showing program paths like on previous slides
- Dataflow Analysis
 - Propagate information through graph, until it is stable

Control Flow Graph

- Representation of all possible program paths
 - Typically inside a method (intra-method)
- Node = Basic Block
 - Straight code section
 - Entry only at the beginning: No label in the middle
 - Exit only at the end: No branch in the middle
- Edge
 - Conditional or unconditional branch

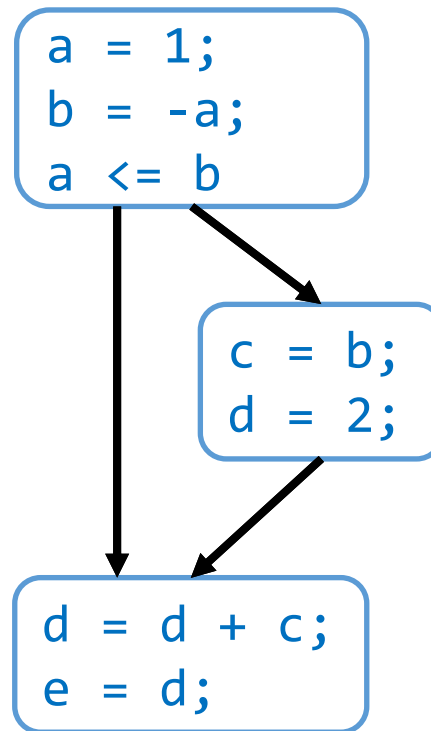
Basic Blocks

- Delimited by branch entry and exit

```
a = 1;  
b = -a;  
if (a <= b) {  
    c = b;  
    d = 2;  
}  
d = d + c;  
e = d;
```

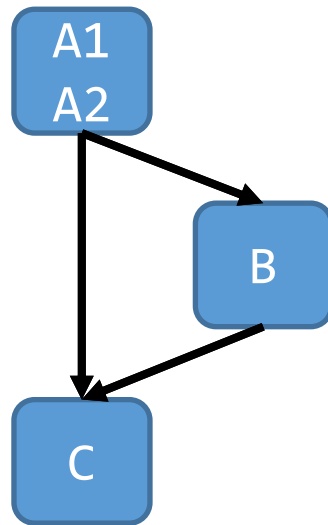
Control Flow Graph (CFG)

- Connected basic blocks according to possible branches

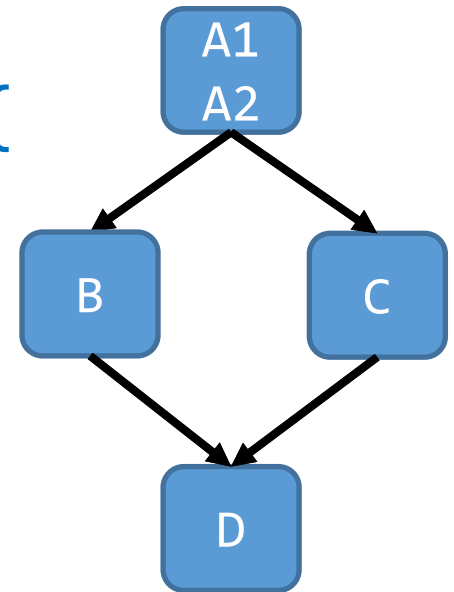


CFG for If-Statement

```
A1;  
if (A2) {  
    B;  
}  
C;
```

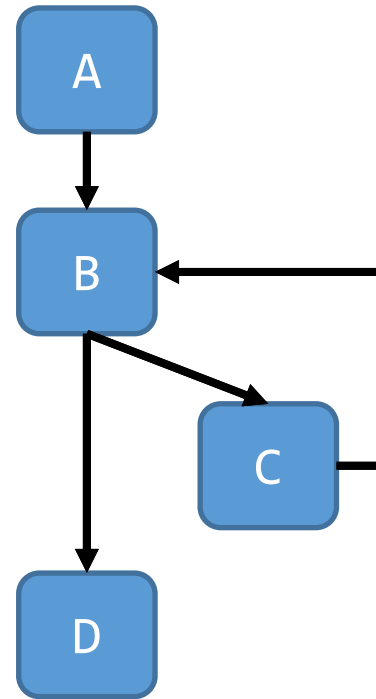


```
A1;  
if (A2) {  
    B;  
} else {  
    C;  
}  
D;
```



CFG for While-Statement

```
A;  
while (B) {  
    C;  
}  
D;
```

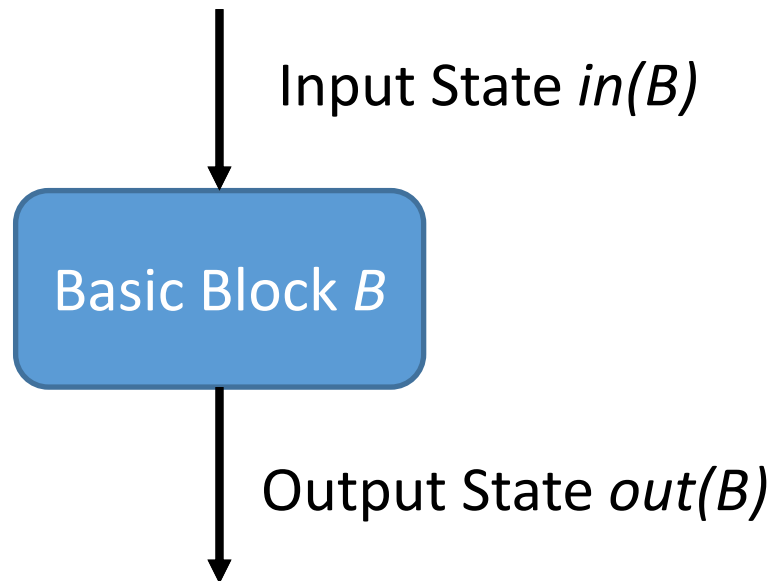


Dataflow Analysis

- Fixpoint iteration over Control Flow Graph
 - Propagate analysis information (state) through blocks
 - Until state is stable for each block (fixpoint)
- Dataflow Analysis is generic
 - Applicable for various use cases
 - State will be defined per use case

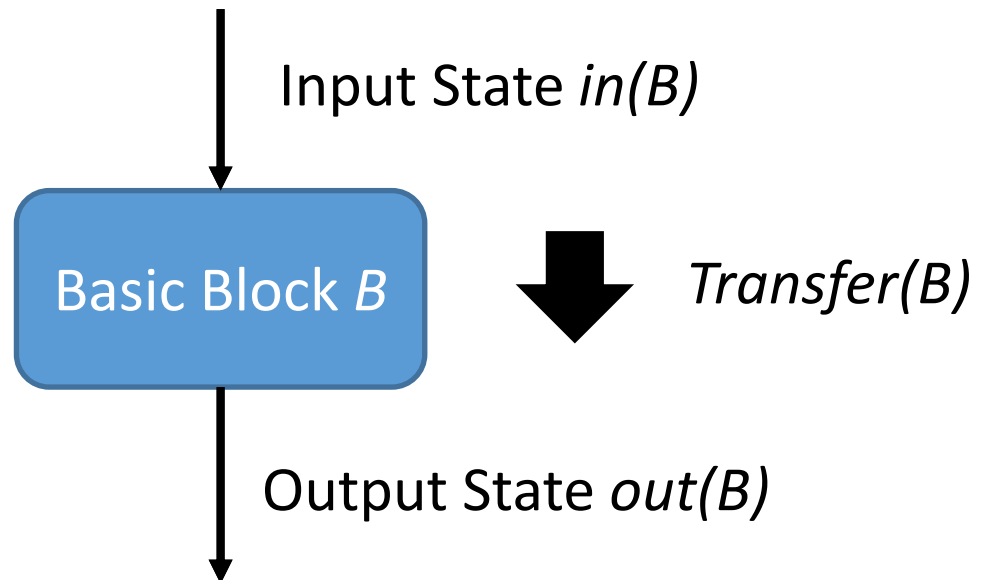
State

- Input state und output state per basic block
- Analysis information before and after the block



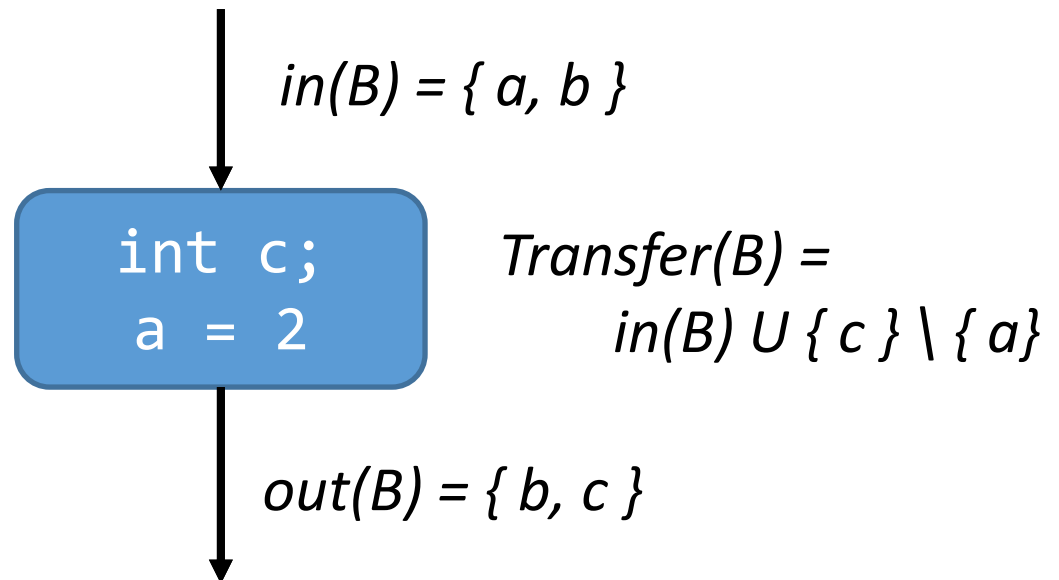
Transfer

- Mapping per block: Input State \rightarrow Output State
- Defines block's effect on analysis information



Analysis Example

- State = Set of uninitialized variables
- Transfer = Add variable declarations, remove assigned variables



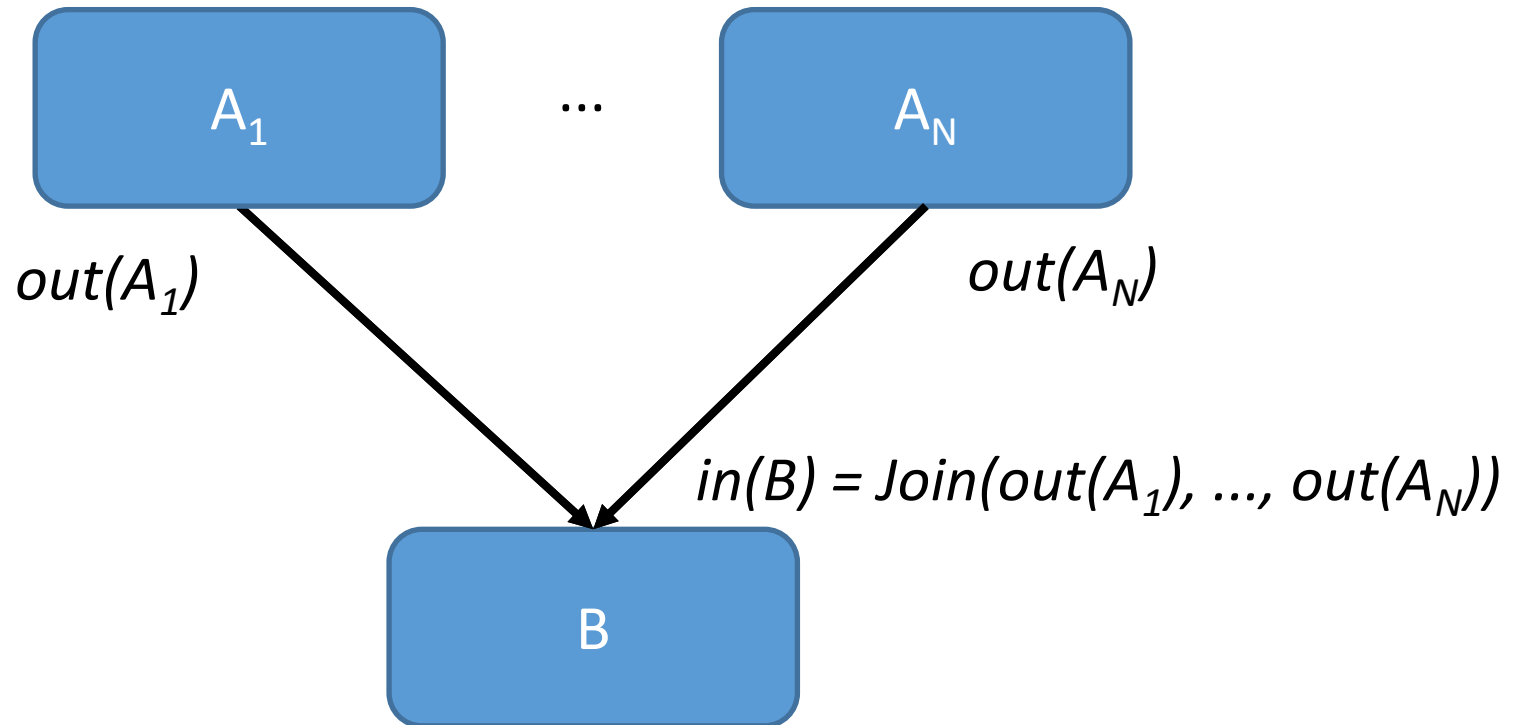
Gen and Kill Set

- Transfer can be described by two sets
- Gen Set: Elements to add
 - Example: Variable declarations
- Kill Set: Elements to remove
 - Example: Assigned variables

$$Transfer(B) = in(B) \cup gen(B) \setminus kill(B)$$

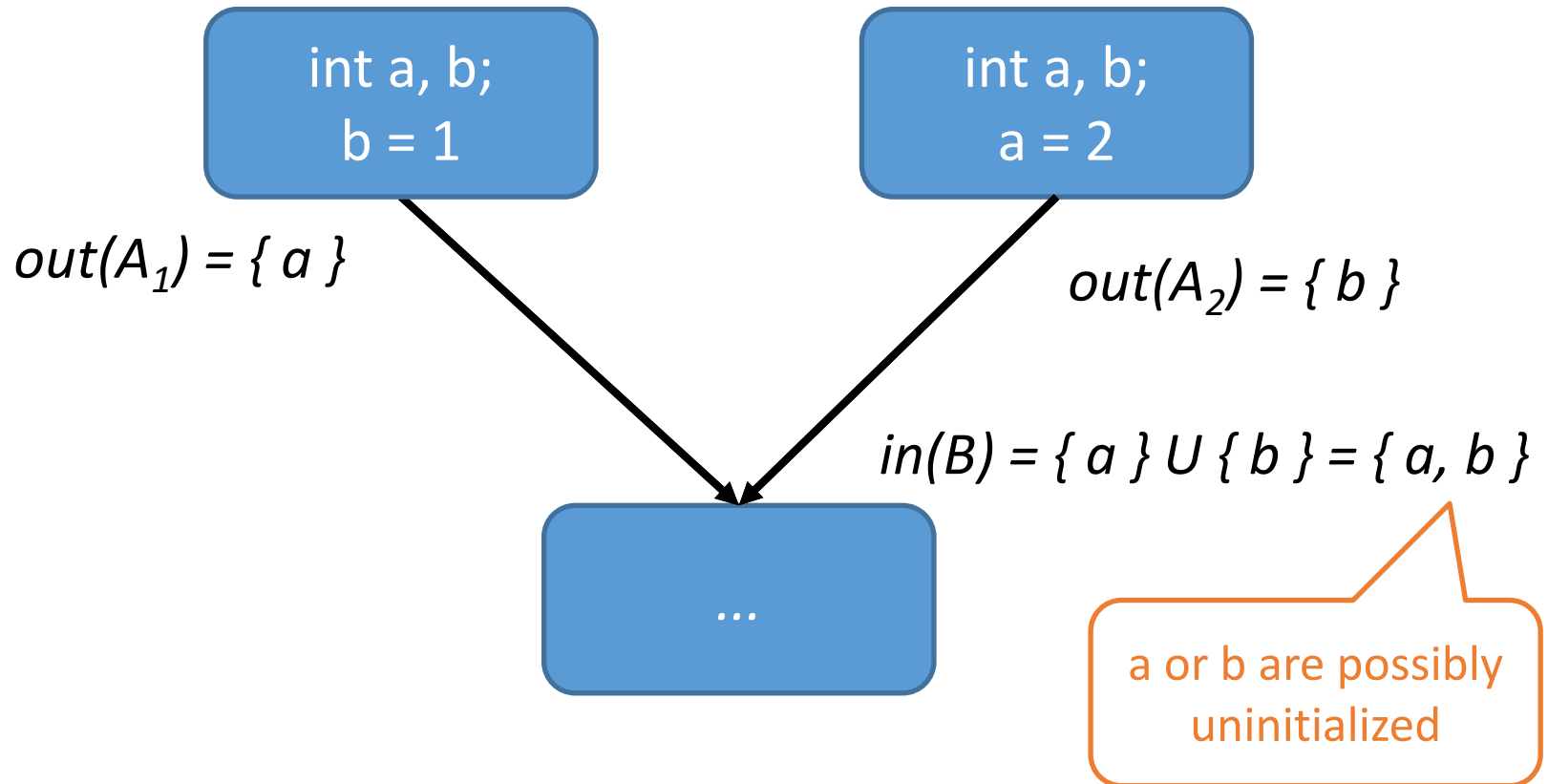
Join

- Combine output state of predecessors to input state of the successor



Analysis Example

- Join = Union set of predecessors



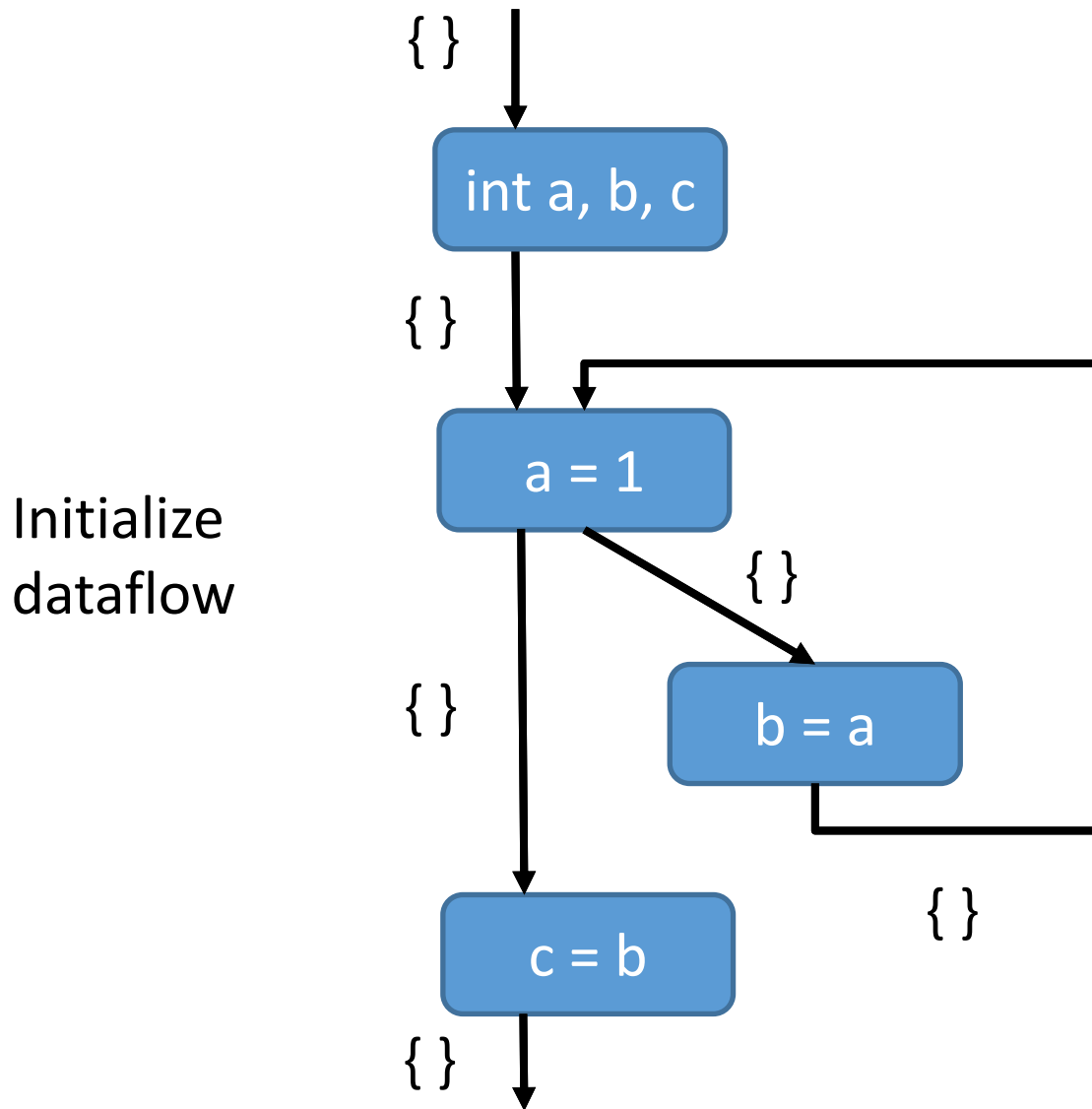
Dataflow Analysis

```
boolean stable;
do {
  stable = true;
  for (var block : graph.allBlocks()) {
    in[block] = join(block.predecessors().outStates());
    var oldOut = out[block];
    out[block] = transfer(in[block]);
    if (!out[block].equals(oldOut)) {
      stable = false;
    }
  }
} while (!stable);
```

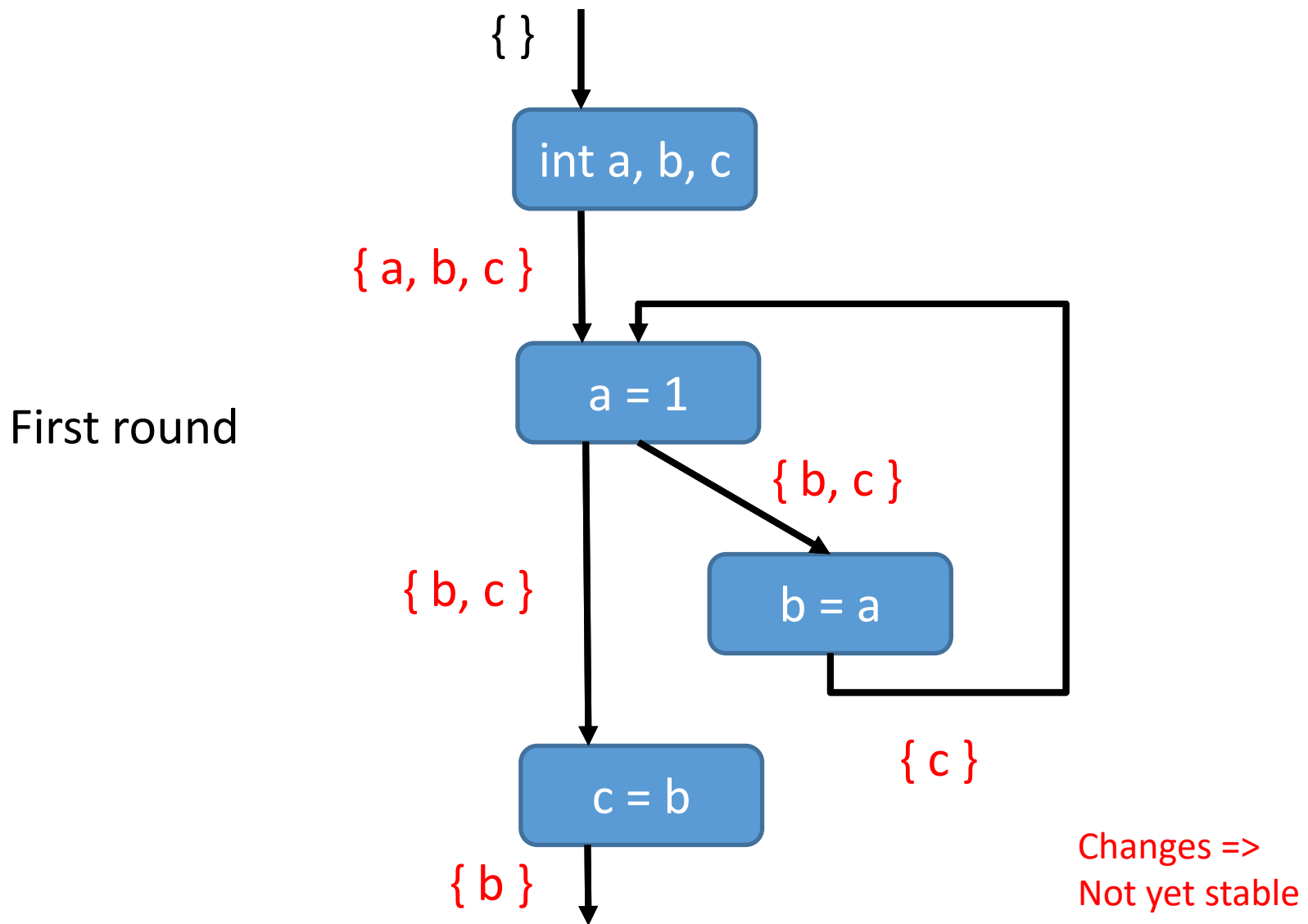


Fixpoint iteration

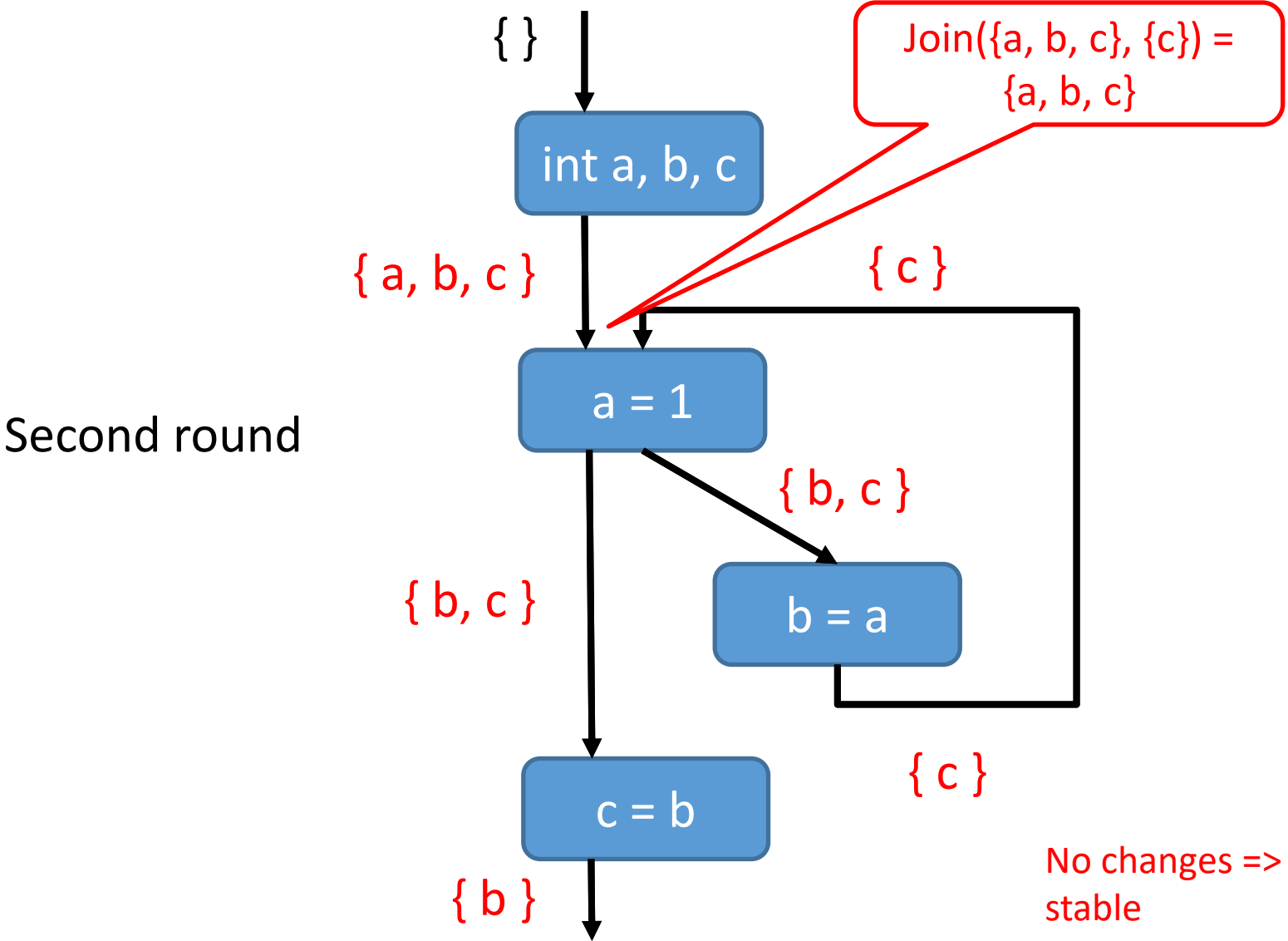
Uninitialized Variable Analysis



Uninitialized Variable Analysis

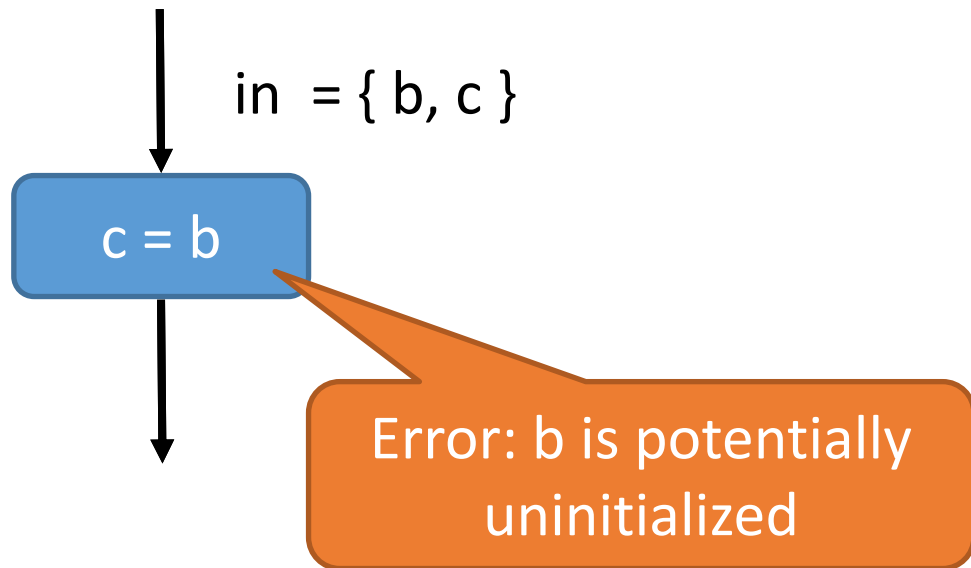


Uninitialized Variable Analysis



Results After Dataflow Analysis

- Use stable input or output states for block properties
- E.g. compiler error for uninitialized reads



Discussion

- Conservative analysis
 - Considers all possible syntactic paths
- Context-free analysis
 - All paths are selected, regardless of their condition
- Error reporting is also conservative
 - It exists at least one path where error could occur
- Fixpoint iteration needs to terminate
 - E.g. if set grows monotonically by joins

Error \Leftrightarrow potentially uninitialized

No error \Leftrightarrow certainly initialized

Revisiting Constant Propagation

- Example of last week

```
a = 1;
if (...) {
    a = a + 1;
    b = a;
} else {
    b = 2;
}
c = b + 1;
```

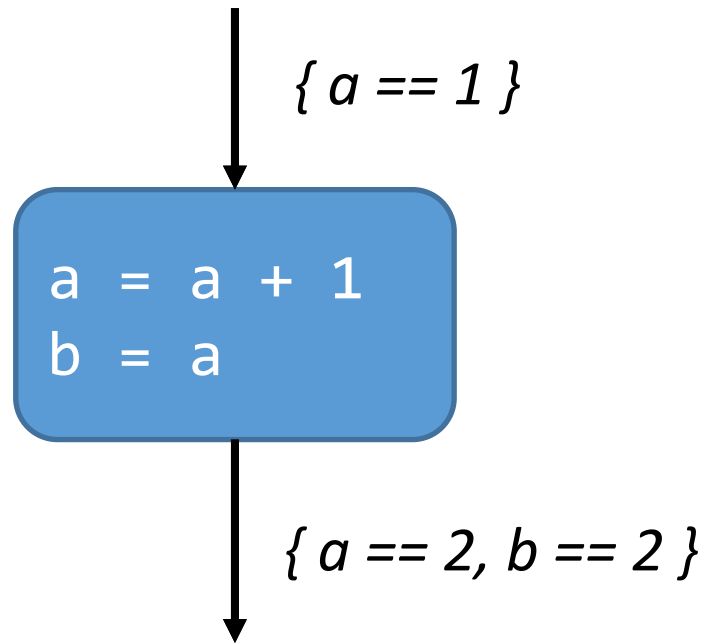


c is certainly 3

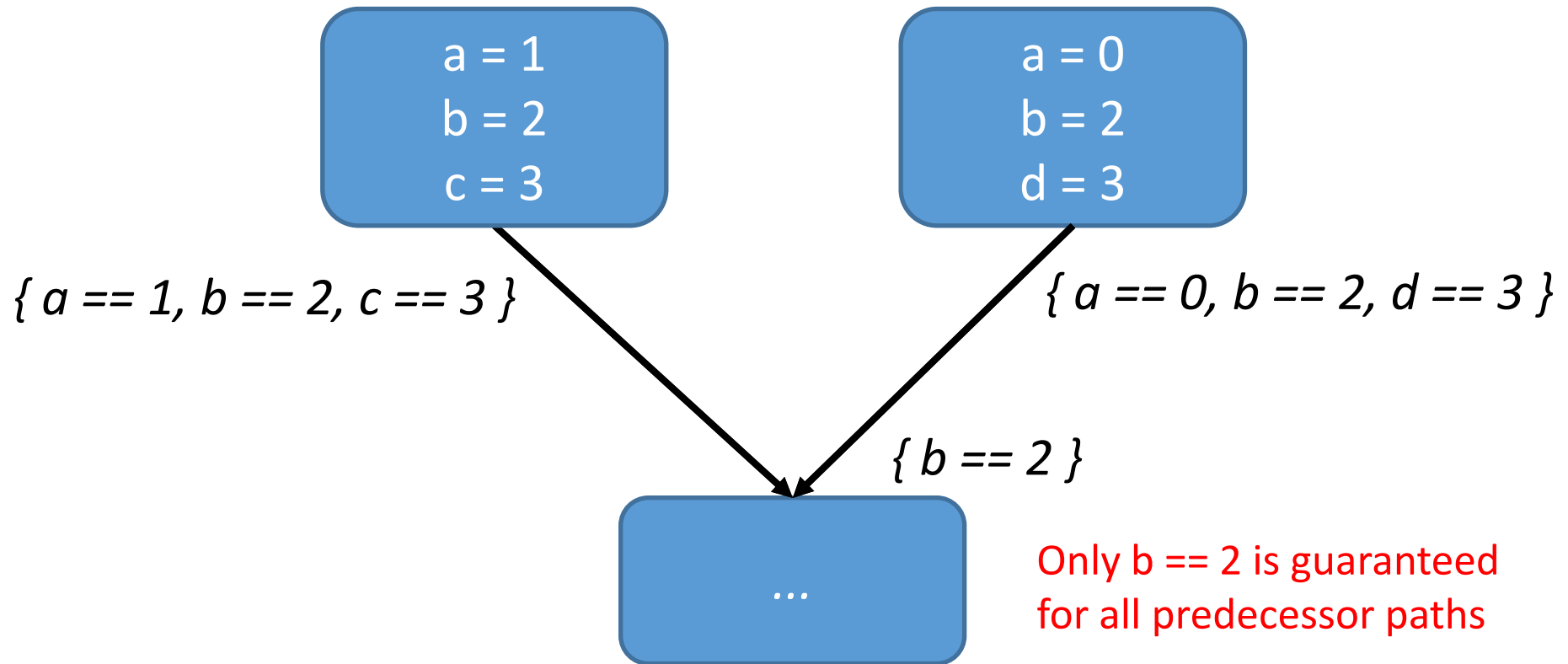
Configuring the Analysis

- State: Variables with their associated constant value
 - { $a == \text{const1}$, $b == \text{const2}$, ... }
- Transfer for $a = E$
 - Kill: Remove $a == \dots$ (if existing)
 - Gen: If E is constant, add $a == E$
- $\text{Join}(X, Y) = X \cap Y$
 - Intersection

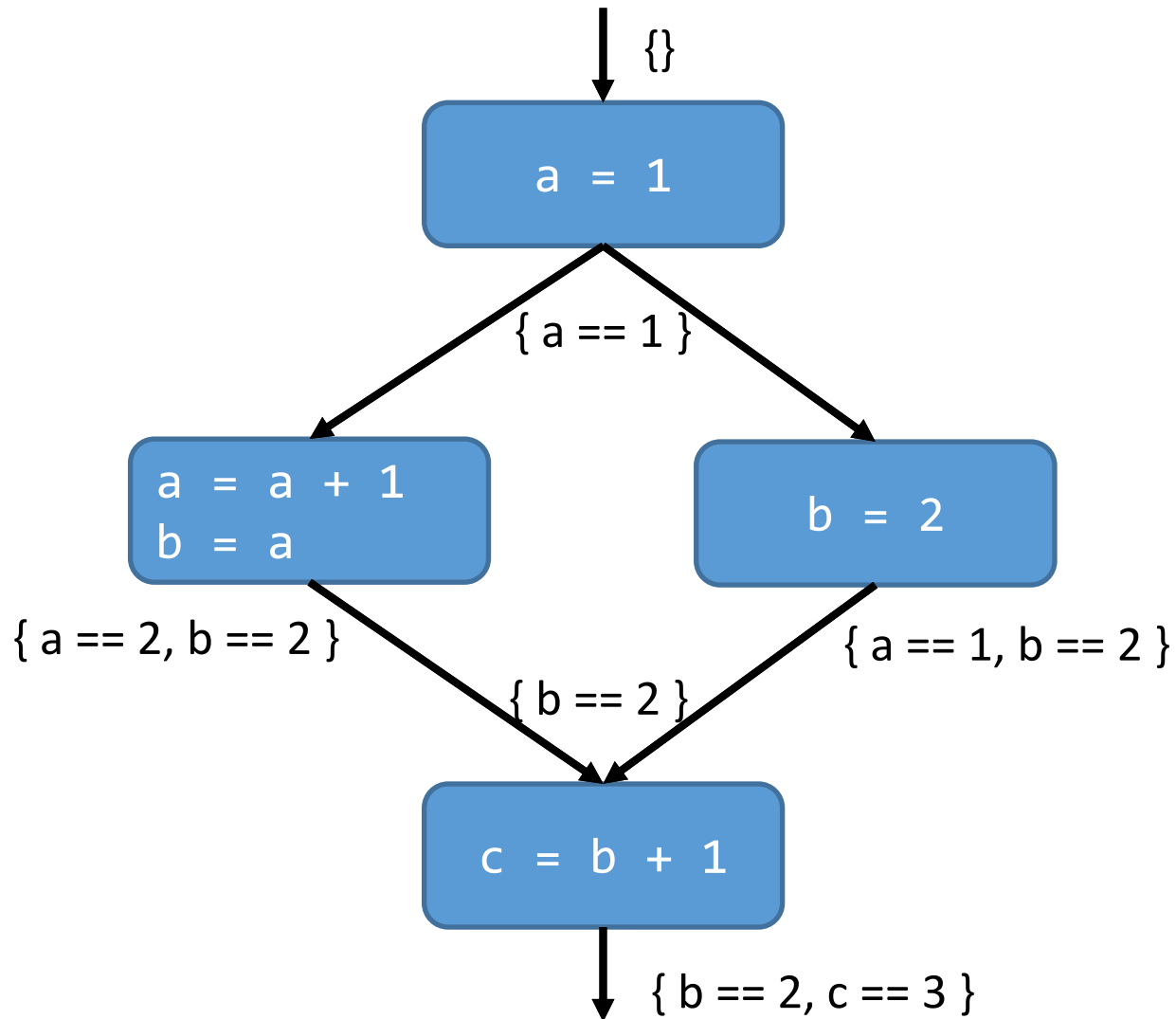
Constant Propagation: Transfer



Constant Propagation: Join



Constant Propagation Example



Review: Learning Goals

- ✓ Understand dataflow analysis as a generic code analysis method
- ✓ Know how to apply it for error detection and optimizations in a compiler

Continued in the next lecture

Further Reading

- Dragon Book, Code Optimization
 - Section 9.2-9.3: Dataflow analysis
 - Section 9.4: Constant propagation
- Optional, if interested
 - F. Nielson, H. R. Nielson, C. Hankin. Principles of Program Analysis, Springer, 2004.



Course 142A Compilers & Interpreters
Code Analysis Continued

Lecture Week 5, Wednesday
Prof. Dr. Luc Bläser

Quiz - Last Lecture

Constant Propagation

```
a = 1;
while (...) {
    if (...) {
        a = a + 1;
        b = a;
    } else {
        b = 2;
    }
    c = b + 1;
}
```



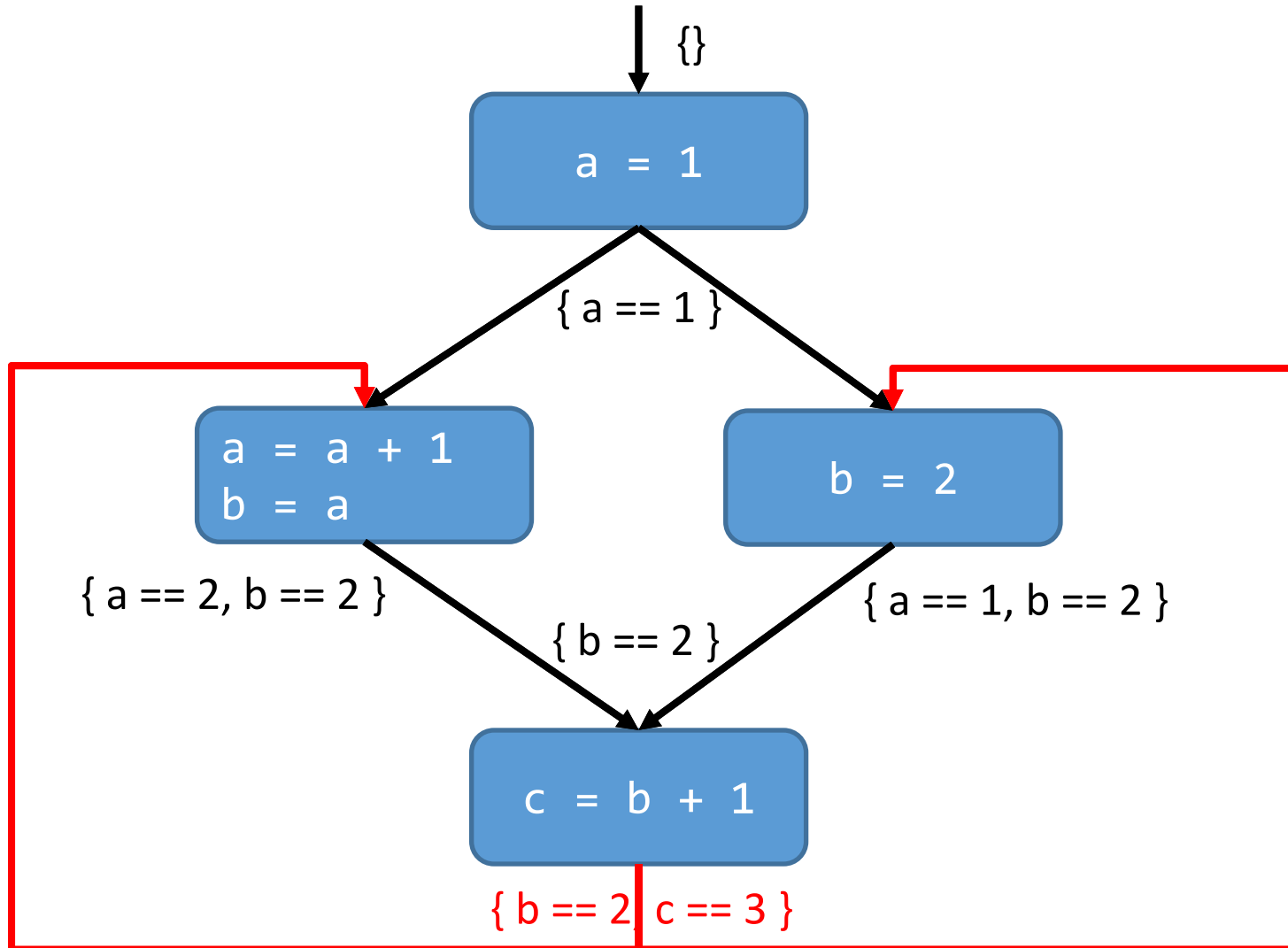
How do we configure the dataflow analysis?

- State, Transfer, Join

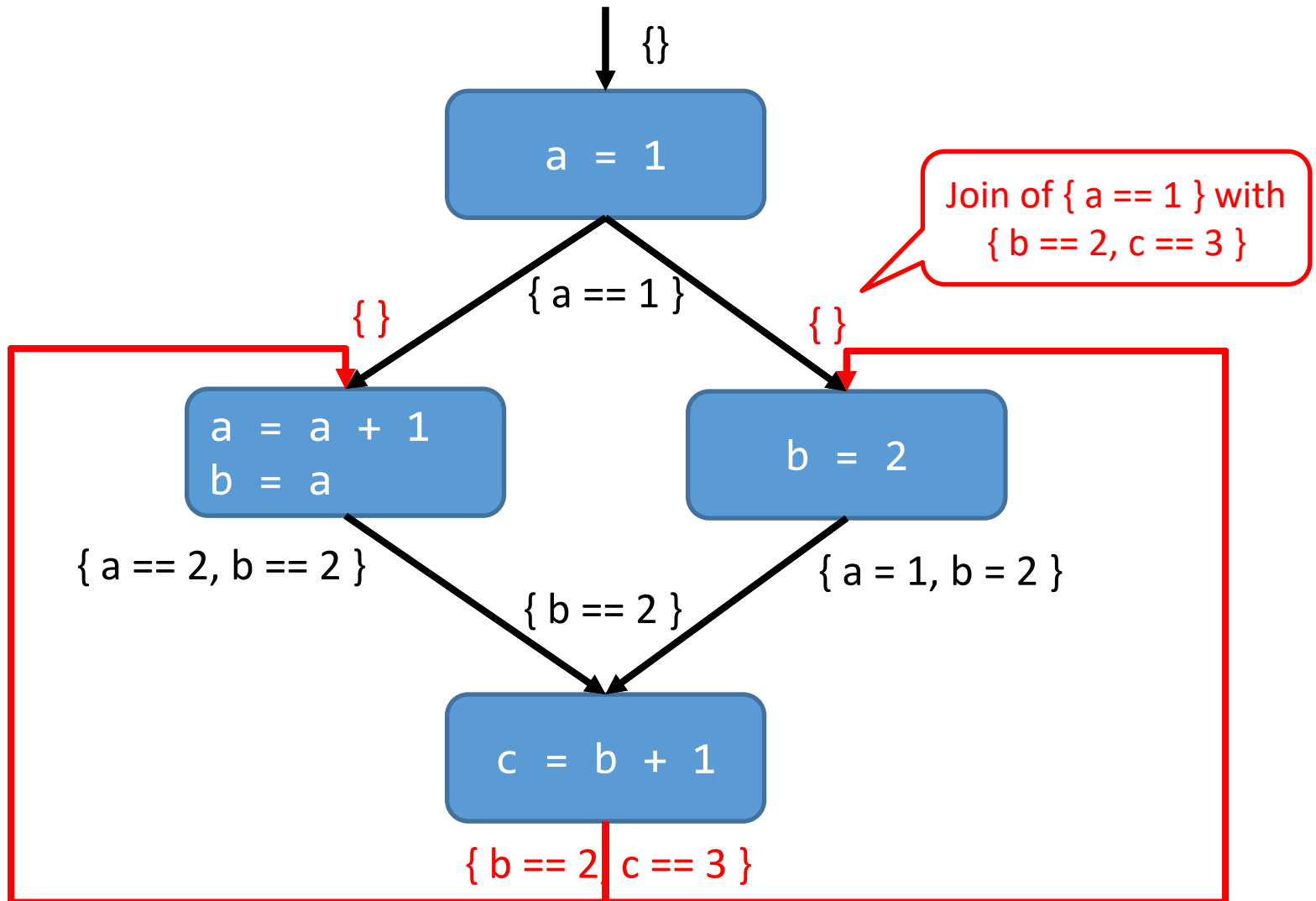
Today's Agenda

- Continue Dataflow Analysis
- Midterm Q&A

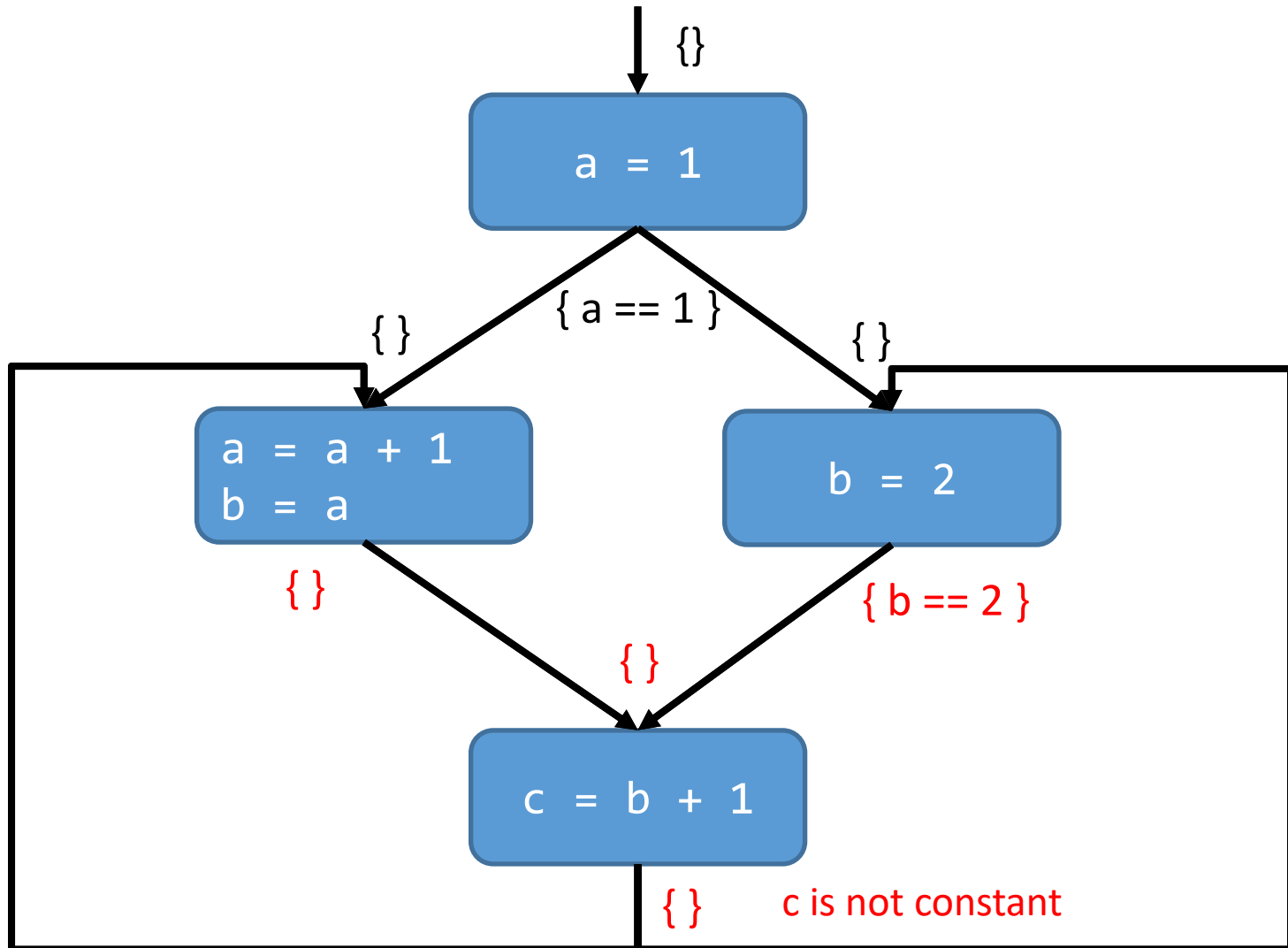
Constant Propagation Scenario



Dataflow Scenario



Dataflow Scenario



Backwards Analysis

- Dataflow analysis can also run backwards: From successors to predecessors
- Transfer: Out State \rightarrow In State
- Join: In states of successors \rightarrow out state of predecessor

Example: Live Variables

- Variables that may be used later
- Eliminate non-live variables (=dead)

```
a = b;  
b = 2;  
if (...) {  
    b = a;  
    a = 1;  
}  
writeInt(a);
```

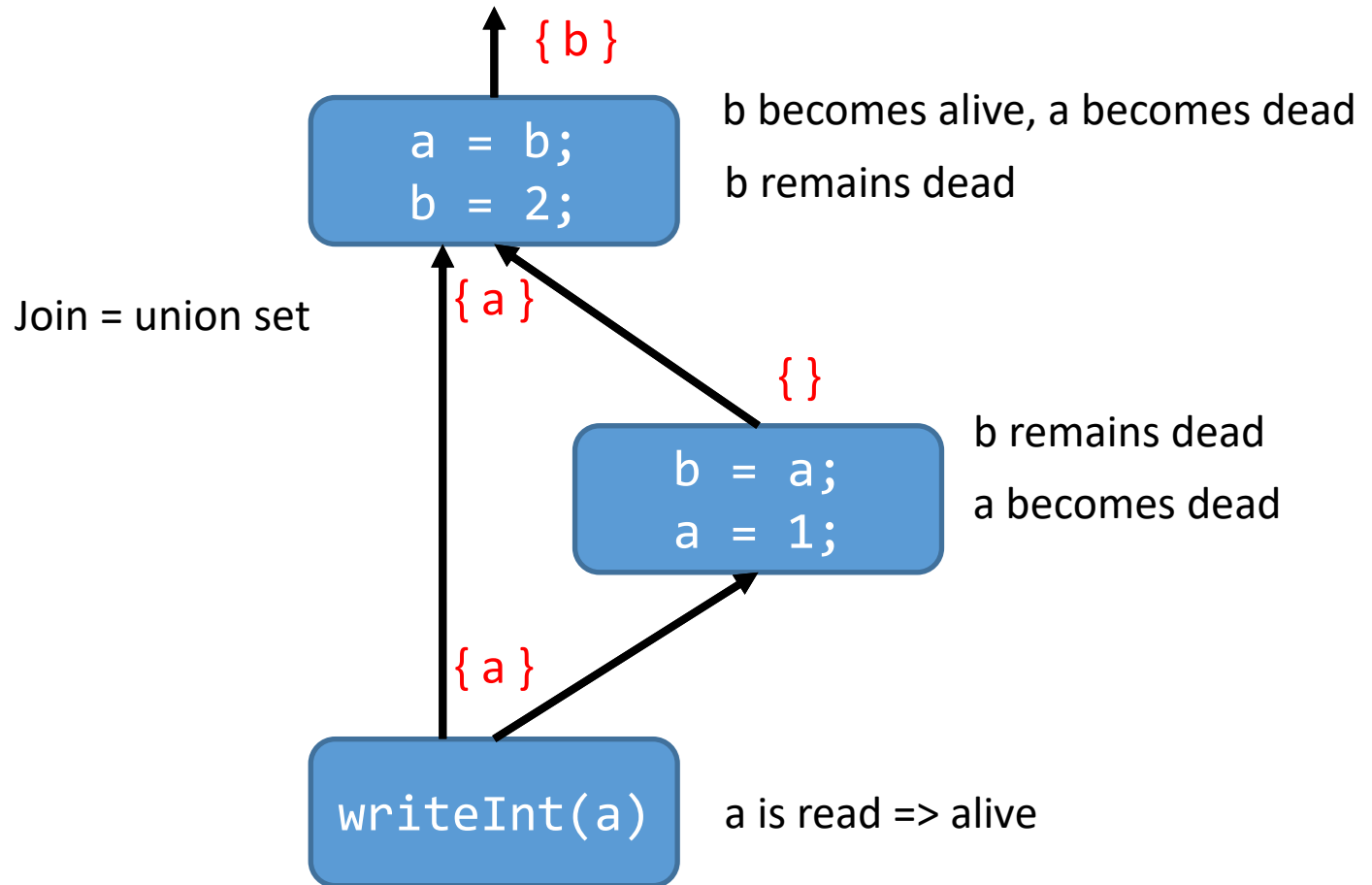


b is hereafter
no longer used

Live Variable Configuration

- Backwards direction
- State: Live variables (variables that may be read)
- Transfer for $a = b \bullet c$:
 - Gen: If a is alive in succeeding code, so are also b and c
 - Kill: a is no longer alive
- $\text{Join}(X, Y) = X \cup Y$

Backwards Analysis



Dead Code Elimination

- Remove assignments to non-live (dead) variables

```
a = b;  
b = 2;  
if (...) {  
    b = a;  
    a = 1;  
}  
writeInt(a)
```



```
a = b;  
if (...) {  
    a = 1;  
}  
writeInt(a)
```

Summary

- Dataflow is generic
- Allows different configurations

| | Join = union | Join = intersection |
|----------|-------------------------|----------------------|
| Forward | Uninitialized Variables | Constant Propagation |
| Backward | Live Variables | (Busy Expressions) |

Expressions, that are computed on all paths

Further Reading

- Dragon Book, Code Optimization
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